¹ Supporting Information for

² "SERMeQ model produces a realistic upper bound on calving re-

treat for 155 Greenland outlet glaciers"

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Additional Supporting Information (Files uploaded separately)

 Table S1, a list of all Greenland outlet glaciers in the MEaSUREs dataset with their glacier ID number, name(s), optimal yield strength found, and notes on inclusion in the analysis. The note "Flagged for bad flowline trace" indicates glaciers that required manual intervention to complete data processing, but which are now included in the analysis.

17 Introduction

¹⁸ Text S1. Ice dynamics in SERMeQ

The ice dynamics in our model are based on a perfectly-plastic limiting case of a viscoplastic rheology (Bassis & Ultee, 2019). This rheology describes a glacier with two characteristic timescales: viscous deformation (slow) and mass loss by calving (fast). Modifications to the simple plastic formulation allow calving at a grounded ice-water interface (Ultee & Bassis, 2016) and interaction between multiple tributary glaciers (Ultee & Bassis, 2017). By requiring instantaneous stress balance across the glacier terminus, this formulation finds that the ice thickness H_{terminus} at a given terminus position, in water of depth D, is limited by the yield strength and cannot exceed the yield thickness,

$$H_{\rm y} = 2\frac{\tau_{\rm y}}{\rho_{\rm i}g} + \sqrt{\frac{\rho_{\rm w}}{\rho_{\rm i}}D^2 + 2\frac{\tau_{\rm y}}{\rho_{\rm i}g}},\tag{S1}$$

with τ_y the yield strength of glacier ice, $\rho_i = 920 \text{ kg m}^{-3}$ the density of glacier ice, $\rho_w = 1020 \text{ kg m}^{-3}$ the density of seawater, and $g = 9.81 \text{ m s}^{-2}$ the acceleration due to gravity (Ultee & Bassis, 2016).

In a perfectly plastic glacier (Nye, 1951), the upstream ice thickness H along a central flowline, with along-flow direction x and ice surface elevation s, is also controlled by the yield strength:

$$H\frac{\partial s}{\partial x} = \frac{\tau_{\rm y}}{\rho_{\rm i}g}.\tag{S2}$$

This approximation corresponds to a case where the glacier bed is (nearly) plastic and the glacier stress balance is dominated by shear at the glacier bed and valley walls—appropriate for most Greenland outlet glaciers. We also account for longitudinal

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stresses in a boundary layer near the terminus, where they are more likely to be
 important (Bassis & Ultee, 2019).

Finally, we use mass continuity to derive an expression for the rate of terminus advance or retreat due to calving (see Text S2, below). With each change in terminus position, we calculate a new surface profile according to Equations S1-S2, and we integrate the changes in ice volume above buoyancy throughout the catchment to deduce a contribution to global mean sea level. Figure S1 shows an example sequence of glacier profiles and corresponding sea level contribution as calculated by SERMeQ.

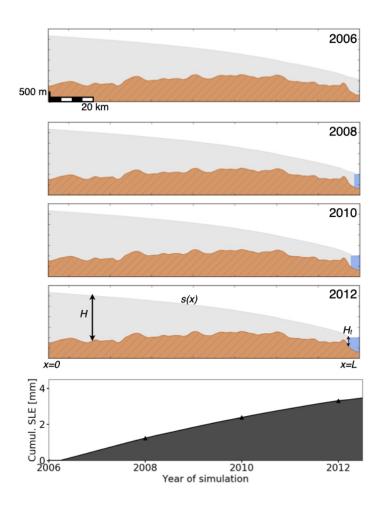


Figure S1. Surface profiles produced by SERMeQ along a flowline in the central part of Ser-33 meq Kujalleq's catchment, with corresponding cumulative sea level contribution (SLE) below. 34 Profiles show glacier ice in grey, bedrock in brown, and fjord water in blue. Spatial scale is in-35 dicated on the 2006 panel and consistent throughout. Labels on 2012 panel indicate along-flow 36 direction x, ice surface elevation s(x), ice thickness H, terminus ice thickness H_t , and terminus 37 location x=L as used in Equations S1-S6. Cumulative SLE on bottom panel reflects catchment-38 integrated loss of ice volume above buoyancy converted to an equivalent volume of seawater and 39 distributed over the area of the global ocean. 40

Despite the simplicity of the model, preliminary experiments have shown promise in reproducing both surface elevation profiles and advance/retreat rates of glaciers in Alaska and Greenland (Ultee & Bassis, 2016, 2017). However, our model only applies to grounded glaciers and cannot simulate the dynamics of floating ice tongues or shelves.

⁴⁵ Text S2. Time evolution of the terminus position

Glacier terminus position in SERMeQ evolves in response to near-terminus stretch ing, bedrock topography, and changes in catchment-wide surface mass balance as
 described in Ultee (2018) and Bassis and Ultee (2019). Below is a brief summary
 derivation of the terminus evolution condition as implemented in SERMeQ code.

Let x = 0 represent the ice divide and x = L the terminus, where L = L(t) is the length of the glacier (labelled in Figure S1). The time derivative dL/dt then represents the change in terminus position over time.

Taking the material derivative of the terminus ice thickness $H = H_y$ (constrained by Equation S1), we find

$$\frac{DH}{Dt}\Big|_{x=L} = \frac{DH_{y}}{Dt}$$

$$\left[\frac{\partial H}{\partial t} + \frac{dL}{dt}\frac{\partial H}{\partial x}\right]_{x=L} = \frac{\partial H_{y}}{\partial t} + \frac{dL}{dt}\frac{\partial H_{y}}{\partial x}$$

$$\frac{\partial H}{\partial t}\Big|_{x=L} = \frac{dL}{dt}\left[\frac{\partial H_{y}}{\partial x} - \frac{\partial H}{\partial x}\right]_{x=L}.$$
(S3)

Mass continuity requires

$$\frac{\partial H}{\partial t} + \frac{\partial}{\partial x}(HU) = \dot{a} \tag{S4}$$

where H = H(x,t) is the ice thickness, U = U(x,t) the ice velocity, and $\dot{a} = \dot{a}(x,t)$ the net ice accumulation rate, for all (x,t).

Substituting equation (S4) into (S3), we find

$$\dot{a} - H\frac{\partial U}{\partial x} - U\frac{\partial H}{\partial x} = \frac{dL}{dt} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x}\right]_{x=L}$$
(S5)

$$\frac{dL}{dt} = \frac{\dot{a} - H\frac{\partial U}{\partial x} - U\frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x}},$$
(S6)

with all terms of equation (S6) evaluated at x = L, the terminus of the glacier (compare with Equation 54 of Bassis and Ultee (2019)). With the exception of ice accumulation wate \dot{a} all terms are determined by the pheelectric of ice

 $_{57}$ rate \dot{a} , all terms are determined by the rheology of ice.

Upstream from the terminus, we assume a plastic yielding layer at the bed of the glacier. A perfectly plastic glacier would have a rigid ice plug above the yielding layer, but the perfect plastic approximation is a limiting case of several other rheologies that could be used to describe the slow deformation of ice in a pseudo-plug (e.g. Balmforth et al., 2006). Here we choose to describe the slow deformation of intact ice with the familiar Glen's flow law. At the terminus, as in Ultee and Bassis (2016, 2017), we require a vertical yield surface to describe the more rapid motion of fractured, disarticulated ice as it calves away from the intact glacier. This implies that the effective stress in a region of length δ upstream from the terminus is within ϵ of the yield strength τ_y . Near the terminus, we have

$$\frac{\partial U}{\partial x} = \dot{\varepsilon}_{xx} = A\tau_{xx}^{n} \\
= A\tau_{y}^{n},$$
(S7)

where flow law exponent n = 3 and A is the flow rate parameter of Glen's flow law.

We integrate equation (S4) in x to find

$$\int_{0}^{L} \frac{\partial H}{\partial t} \,\mathrm{d}x + (HU)|_{x=L} = \int_{0}^{L} \dot{a} \,\mathrm{d}x \tag{S8}$$

$$U(x = L) = \frac{1}{H_{\text{terminus}}} \int_0^L \left[\dot{a} - \frac{\partial H}{\partial t} \right] \, \mathrm{d}x,\tag{S9}$$

and by the chain rule $\frac{\partial H}{\partial t} = \frac{\partial H}{\partial L} \frac{dL}{dt}$. Separating the integral in equation (S9) and expanding $\frac{\partial H}{\partial t}$ gives

$$U(x = L) = \frac{\dot{\alpha}L}{H_{\text{terminus}}} - \frac{dL}{dt} \frac{1}{H_{\text{terminus}}} \int_0^L \frac{\partial H}{\partial L} \, \mathrm{d}x, \tag{S10}$$

where $\dot{\alpha} = \frac{1}{L} \int_0^L \dot{a} dx$ is the spatially-averaged ice accumulation rate along the flowline. 59

We now substitute our expressions (S7, S10) in to equation (S4) and rearrange to find

$$\frac{dL}{dt} = \frac{\dot{a} - A\tau_{y}^{3}H_{\text{terminus}} + \frac{\alpha L}{H_{\text{terminus}}}\frac{\partial H}{\partial x}}{\frac{\partial H_{y}}{\partial x} - \frac{\partial H}{\partial x}\left(1 - \frac{1}{H_{\text{terminus}}}\int_{0}^{L}\frac{\partial H}{\partial L}\right)}.$$
(S11)

We implement a discretized version of Equation S11 to describe the time evolution 60 of glacier terminus position in SERMeQ. 61

Text S3. The role of adjustable parameters 62

In this work, we aimed to validate the upper bounding approach of SERMeQ 63 using independent, uncalibrated predictions of terminus position. As such, we did not 64 adjust any parameter to match observed retreat rates. For other applications it may be 65 desirable to manipulate the yield strength $\tau_{\rm y}$ or the ice temperature T. Adding a tuning 66 parameter would reduce the mismatch between model predictions and observations, 67 but at the steep cost of eliminating independent comparison between model predictions 68 and observations. 69

Yield strength $\tau_{\rm v}$ 70

For each glacier, we optimize the yield strength τ_y to find the best fit between 71 a reconstructed and observed centerline surface elevation profile. Glaciers with flatter 72 surface slopes, including those close to flotation, are best fit by lower values of $\tau_{\rm v}$. 73 Steeper surface slopes are better fit by higher values of the yield strength. The opti-74 mization procedure is discussed in detail in Ultee and Bassis (2016). The optimal value 75 of τ_y found for each glacier is listed in Supplementary Table 1. There is no correlation 76 between optimal yield strength and glacier latitude, and no other spatial pattern is 77 evident. 78

Figure S2 shows a histogram of the best-fit values of $\tau_{\rm v}$ obtained for the Greenland 80 outlets we simulated. A central peak in the distribution shows that approximately 1/381 of the glaciers we simulate have an optimal yield strength between 125 kPa and 150 82 kPa. A smaller peak shows that there are also several glaciers in our set best fit by 83 yield strengths between 5 kPa-25 kPa. 84

In this work, we have used a single value of τ_y at both the ice-bed interface 85 and the calving front. It is plausible that the ice-bed interface could be deforming 86 more readily than the pure ice at the calving front, for example if the glacier bed is 87 composed of saturated marine sediments or if the ice is very close to flotation. Such a 88 case would lead to low ice surface slopes and a low optimal value of $\tau_{\rm v}$, even though 89 pure ice throughout the glacier may be stronger. We discuss the case of $\tau_{bed} < \tau_{ice}$ in 90 Bassis and Ultee (2019).

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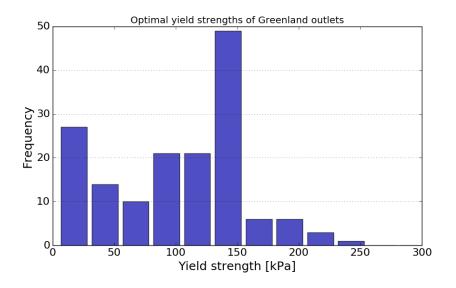


Figure S2. Histogram of optimal yield strength value found for each glacier.

$_{92}$ Ice temperature T

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The ice temperature T is used to select an appropriate value of the flow-rate parameter A in Glen's flow law. To validate our upper bounding approach, we use a best-guess ice temperature $T=-10^{\circ}$ C, constant in space and time, and do not optimize for its value. In our previous work, we have found that warmer ice $(T=-2^{\circ}$ C) is softer and more prone to rapid retreat. Conversely, colder ice $(T=-30^{\circ}$ C) is stiffer and retreats more slowly (Ultee, 2018).

For applications prioritizing a close match between simulated and observed retreat, the ice temperature (and/or yield strength) can be adjusted for each glacier. Choosing a lower ice temperature can mitigate some dramatic overestimates of retreat, as shown for the example of Helheim Glacier in Figure S3a. Manipulating the ice temperature does sacrifice upper bound performance. Simulation of all outlets with $T=-30^{\circ}$ C, illustrated in Figure S3b, underestimated retreat twice as often as simulation with $T=-10^{\circ}$ C (shown in Figure 2).

112 Text S4. Inclusion of submarine melt

We do not explicitly simulate loss of ice from glacier termini by submarine melting. Rather, we have constructed an upper-bound estimate of retreat that is consistent with high submarine melt rates. Our requirement that effective stress near the glacier terminus must equal the yield strength of ice (see Text S1) makes an implicit constraint on the submarine melt rate, because the rate of submarine melt shapes the stress field near glacier termini (Ma, 2018; Ma & Bassis, 2019). There are three cases to consider:

Case I The submarine melt rate is very small compared with the terminus velocity, $u_s \ll u_t$. In this case, the terminus would be able to advance and thin episodically. However, advance and thinning would lower the effective stress at the glacier terminus, such that it would fall below the yield strength of ice and no longer satisfy our criterion. The model construction therefore disallows Case I.

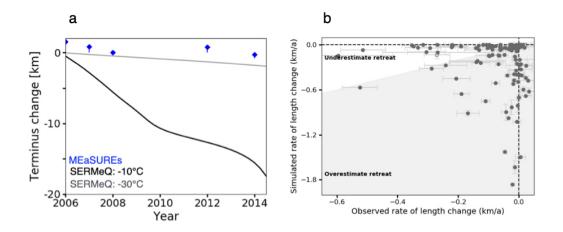


Figure S3. Effect of ice temperature in simulated retreat. (a) Observed and simulated retreat of Helheim Glacier using two different values of T. Black curve indicates SERMeQ-simulated terminus positions with $T=-10^{\circ}$ C, as in main text (Figure 3b). Grey curve indicates SERMeQsimulated termini with $T=-30^{\circ}$ C. Blue markers indicate MEaSUREs observations. (b) Observed versus simulated retreat rate for all glaciers simulated with $T=-30^{\circ}$ C-contrast with main text Figure 2.

124	Case II The submarine melt rate is comparable to the terminus velocity, $u_s \sim u_t$. In
125	this case submarine melt would balance the tendency of ice near the terminus to
126	stretch and thin, maintaining the terminus ice thickness at the yield thickness.
127	Case III The submarine melt rate is very large compared with the terminus veloc-
128	ity, $u_s \gg u_t$. In this case, the erosion of the terminus by high submarine melt
129	would create an overhang and promote calving, with an average rate of over-
130	hang calving equal to the submarine melt rate (Ma & Bassis, 2019). When the
131	overhanging ice calves, the exposed grounded ice face will
132	• have thickness equal to the yield thickness, satisfying our model construction
133	and maintaining an active calving front;
134	• be thinner than the yield thickness, such that the effective stress is lower than
135	the yield strength, whereby calving ceases and the terminus thickens until the
136	effective stress is once again high enough to calve; or
137	• be thicker than the yield thickness, such that effective stress momentarily
138	exceeds the yield strength and the ice quickly crumbles;
139	as described in Bassis and Ultee (2019). The effect over the months to years
140	considered in SERMeQ (as opposed to the hours to days considered in finer-scale
141	process models) is to maintain a grounded terminus at the yield thickness.
142	Both Cases II and III are consistent with our assumption that there is a yielding
142	boundary layer at the glacier front that constrains the terminus ice thickness. The

boundary layer at the glacier front that constrains the terminus ice thickness. The maximum rate of length change computed in Equation 1 is compatible with both cases, and the ice mass lost in each time step can be considered a combination of mass lost to calving and to submarine melting.

The upper-bound retreat rate that we have sought in this work does not require explicit simulation of the submarine melt rate. Nevertheless, future adaptations of our method to simulate calving in larger-scale models may seek to add a mechanism for forcing by time-varying submarine melt. We suggest that those efforts begin by allowing submarine melt rate u_s to modify the terminus velocity, U in Equation 1,

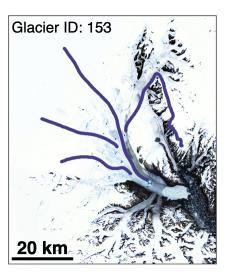


Figure S4. Network of flowlines on Kangerlussuaq Glacier, MEaSUREs Glacier ID 153, as
 defined with our tracing and filtering algorithm.

with the understanding that doing so may introduce scenarios that are incompatible with our original assumptions.

¹⁵⁴ Text S5. Flowline network selection

We apply our depth-integrated, width-averaged model on a network of interacting 155 glacier flowlines, as described in Ultee and Bassis (2017). Previous applications have 156 used flowlines selected by hand (Ultee & Bassis, 2016; Ultee, 2018) or by an automated 157 method that detects valley walls of mountain glacier networks (Kienholz et al., 2014; 158 Ultee & Bassis, 2017). Neither method is suitable for the hundreds of Greenland 159 outlet glaciers we consider here. It is impractical to select hundreds of flowlines by 160 hand, and outlets of the Greenland Ice Sheet, unlike mountain glaciers, expand to a 161 nearly featureless catchment upstream with no valley walls to aid in flowline selection. 162 We therefore apply a new selection algorithm based on tracing ice surface velocity. 163

We begin with a surface velocity composite covering the entire ice sheet (ENVEO, 166 2017). For each glacier included in the MEaSUREs dataset (Joughin et al., 2015, up-167 dated 2017), we extract all points observed along the 2006 terminus position. We then 168 trace each point up the surface velocity field until a pre-determined minimum velocity 169 cutoff (identical for all glaciers); our viscoplastic approximation is most suitable near 170 the glacier terminus (Ultee & Bassis, 2017; Bassis & Ultee, 2019), so we do not extend 171 our simulated catchments all the way to the ice divide. Finally, we filter the set of 172 full-length flowlines so that the most central flowline is defined as the "main trunk". 173 The parallel portions of the remaining flowlines are trimmed and network intersec-174 tions defined where the angle between flowlines exceeds a threshold value (identical 175 for all glaciers). The code used in network selection is available in our public GitHub 176 repository, and an example network is shown in Figure S4. 177

The tracing and filtering of flowlines from surface velocity is prone to error where the velocity dataset is noisy or includes holes. Errors in flowline tracing generally become apparent in later data-processing steps, for example if no optimal yield strength value can be found. Networks affected by such errors include the note "Flagged for bad flowline trace" in Table S1.

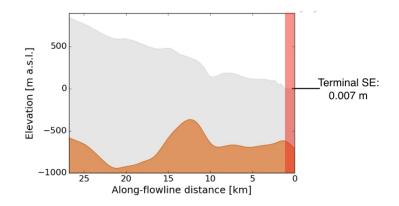


Figure S5. Near-terminus bed topography of Helheim Glacier. Brown filled region shows glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017). Note 10:1 exaggeration in vertical scale. A red overlay indicates floating ice that was removed in our simulation. Annotation at figure left indicates the ice surface elevation at the terminus as recorded in Morlighem et al. (2017), further evidence that the initial terminus could not have been grounded ice.

183 Text S6. Sources of error

As described in the main article text, 40% of terminus positions simulated by 199 SERMeQ fall within the range of observed terminus position for the same year. Be-200 cause SERMeQ is sensitive to bed topography features (Ultee, 2018) and is forced by 201 climate reanalysis data, model performance will generally be best where those data 202 products are most accurate. The agreement between modelled and observed retreat 203 of Sermeq Kujalleq (glacier ID 3, also called Jakobshavn Isbræ, main text Figure 3c), 204 where bed topography has been especially well examined by previous glaciological 205 studies, illustrates this point. 206

We compared three factors hypothesised to contribute to disagreement between 207 simulated and observed retreat rates (henceforth "model mismatch") across all glaciers 208 simulated: length of floating ice removed, error in bed topography, and error or missing 209 data in the ice surface velocity traced to produce the flowlines. Figure S6 shows the 210 model mismatch (y-axis) and the magnitude of each factor relative to its Greenland-211 wide mean (grey polygons). None of the three factors correlates directly with model 212 mismatch. However, glaciers with greater model mismatch tend to have at least one 213 comparatively large contributing factor. 214

The uncertainty in surface mass balance cannot be assessed quantitatively from 215 HIRHAM datasets. However, we have separated the glaciers in Figure S6 into regions 216 to highlight qualitative differences based on Lucas-Picher et al. (2012). Model mis-217 match is generally low on the West Coast and in the Southeast, where Lucas-Picher 218 et al. (2012) show no systematic bias in HIRHAM and a high density of weather 219 stations available to evaluate it. SERMeQ model mismatch is higher, and the pro-220 portion of glaciers with sufficient data for simulation is lower, in the Northeast and 221 Scoresby-Sermilik regions. In the Northeast region, HIRHAM consistently overesti-222 mates surface temperature and tends to underestimate accumulation, which suggests 223 that the resulting surface mass balance may be systematically underestimated. In the 224 Scoresby-Sermilik region, Lucas-Picher et al. (2012) shows only one weather station 225 to validate HIRHAM, which leaves the surface mass balance less constrained than in 226 other areas of the ice sheet. 227

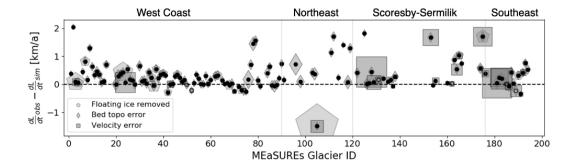


Figure S6. Difference in observed versus simulated retreat rates, and sources of input data 190 error, for each glacier simulated. Dots indicate the difference $\frac{dL}{dt}_{obs}$ - $\frac{dL}{dt}_{sim}$, where dL/dt is the 191 rate of terminus position change as shown in main text Figure 3. Shaded polygons scale to the 192 relative value of each possible source of input error: mean stated error in BedMachine topogra-193 phy (ranging 14-610 m), stated standard deviation in ice surface velocity used to define networks 194 (ranging 0.026-7.3 m/d, with data gaps assigned standard deviation 10 m/d), and length of float-195 ing ice tongue removed (ranging 0-18 km). SERMeQ overestimates the true rate of retreat for 196 points above the x-axis and underestimates for points below. Vertical dividers indicate regions, 197 labeled at the top of the figure. 198

It is our aim to produce an upper bound on outlet glacier retreat and associated 228 mass loss. We demonstrated in Bassis and Ultee (2019) that Equation 1 is a theoretical 229 bound on the rate of calving retreat. Thus, we anticipate that the rate of retreat 230 simulated by SERMeQ will generally exceed the observed rate of retreat. To support 231 future implementation of this calving-rate bound in our model or others, it is important 232 to understand where it does not perform as expected. There are two cases to consider: 233 (1) the retreat rate simulated by SERMeQ is slower than the rate observed, or (2) the 234 retreat rate simulated by SERMeQ far exceeds the rate observed (by a factor of 5 or 235 more). We describe three illustrative examples here. 236

²³⁷ Mean simulated retreat slower than observed

Main text Figure 3a shows the simulated and observed changes in length for 238 Apuseeq Anittangasikkaajuk (MEaSUREs Glacier ID 137), a small outlet glacier on 239 the east coast of Greenland. Our analysis shows that the mean rate of simulated 240 terminus retreat was 32 m/a, while the mean observed rate of retreat of the terminus 241 centroid was 94 m/a. This is one of only a handful of cases in which the mean observed 242 rate over the 2006-2014 period exceeds the supposed upper-bound rate produced by 243 Equation 1. We note that Apuseeq Anittangasikkaajuk is located in the Scoresby-244 Sermilik region indicated in Figure S6, and it is seldom included in other studies 245 of Greenland outlets. As such, relatively low quality climate input data may affect 246 our simulation of this outlet. However, for Apuseeq Anittangasikkaajuk and almost 247 all (9/10) other cases of underestimated retreat, both observed and simulated retreat 248 rates are small, and the simulated terminus position remains within the observed range 249 of terminus positions. 250

²⁵¹ Mean simulated rate far exceeds observed

Main text Figure 3b shows the simulated and observed changes in length for Hel heim Glacier (MEaSUREs Glacier ID 175), a large and well-studied outlet in southeast
 Greenland. The satellite-derived surface velocity field (ENVEO, 2017) included data

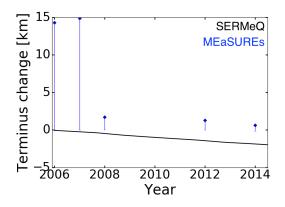


Figure S7. Observed and simulated change in terminus position on Hagen Brae (glacier ID
105). Black curve indicates SERMeQ-simulated terminus positions, while blue markers indicate
MEaSUREs observations. The blue lines show the most-advanced and most-retreated parts of the
terminus projected onto the centerline, and blue diamonds indicate the centroid of the observed
terminus projected onto the centerline. Positive y-axis values indicate terminus positions more
advanced than the initial position; negative y-axis values indicate terminus positions retreated

from the initial position.

gaps that could have produced an unrepresentative flowline network (Text S5), but no network problems were evident on inspection. Bed topography and climate data quality for Helheim Glacier should be comparatively high. Nevertheless, SERMeQ simulates a mean retreat rate of 1840 m/a, which far exceeds the mean observed retreat rate of 136 m/a. We attribute this rapid retreat to features in the bed topography, combined with the no-flotation condition we have implemented in SERMeQ.

The terminus of Helheim Glacier has been observed to float in some years, and 261 was likely floating at the beginning of our simulation period according to bed and 262 surface topography from Morlighem et al. (2017). The glacier bed is more than 600 263 m below sea level and retrograde for several kilometers upstream of the present ter-264 minus, as shown in Figure S5. As explained in main text section 2 and in Ultee and 265 Bassis (2016, 2017), SERMeQ does not allow floating ice tongues to form. Where 266 small tongues are present, we remove them and simulate the first grounded point as 267 the "terminus". In the case of Helheim Glacier, when we removed floating ice, the 268 simulated terminus was pushed onto the retrograde bed, where it began an unstable 269 retreat. In summary, the true near-terminus dynamics and stress field of Helheim 270 Glacier are shaped by the presence of floating ice that interacts with the fjord walls. 271 SERMeQ does not include these dynamics and therefore simulates an upper-bound 272 retreat that could occur in the absence of floating ice. The upper bound retreat rate 273 can be brought closer to the observed rate by adjusting the ice temperature (Figure 274 S3a), but we do not pursue that manipulation here. 275

288

Successive under- and over-estimates within observed period

In a handful of other cases, the rate of retreat observed during a short portion of the observed period exceeds the rate simulated during the same time. Underestimated retreat in one time period is nearly always coupled with overestimated retreat in another period, such that the aggregate effect over the course of the simulation remains an upper-bound estimate of net retreat. For example, between 2007 and 2008, the floating ice tongue of Hagen Brae (MEaSUREs Glacier ID 105) disintegrated (Solgaard et al.,

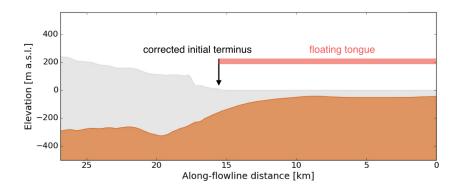


Figure S8. Near-terminus bed topography of Hagen Brae (glacier ID 105). Brown filled region shows glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017). Note 10:1 exaggeration in vertical scale. A red bar shows the length of floating ice that was removed during our model initialization, and a black arrow indicates the first grounded point where SERMeQ could establish an initial terminus.

2020). The resulting observed rate of retreat, more than 10 km/a, far exceeded the 295 rate simulated by SERMeQ (< 1 km/a) over the same period (Figure S4). However, 296 our model initialization had already removed the floating portion of the glacier as of 297 2006, so the SERMeQ-simulated terminus position was still more retreated than the 298 observed. In the subsequent period between 2008 and 2012, SERMeQ slightly overes-299 timated the observed retreat rate. Figure S7 illustrates this history. In Figure S8, we 300 have annotated the floating ice removed upon initialization, the collapse of which was 301 responsible for anomalously high observed retreat between 2007 and 2008. 302

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